- 1. A particle moves on the x-axis so that its velocity at any time  $t \ge 0$  is given by  $v(t) = 12t^2 36t + 15$ . At t = 1, the particle is at the origin.
- 0
  - (a) Find the position x(t) of the particle at any time  $t \ge 0$ .
  - (b) Find all values of t for which the particle is at rest.
  - (c) Find the maximum velocity of the particle for  $0 \le t \le 2$ .
  - (d) Find the total distance traveled by the particle from t = 0 to t = 2.

1994 - AB3

- 3. Consider the curve defined by  $x^2 + xy + y^2 = 27$ .
- (a) Write an expression for the slope of the curve at any point (x, y).
  - (b) Determine whether the lines tangent to the curve at the x-intercepts of the curve are parallel. Show the analysis that leads to your conclusion.
  - (c) Find the points on the curve where the lines tangent to the curve are vertical.

1994 - AB4

- 4. A particle moves along the x-axis so that at any time t > 0 its velocity is given by  $v(t) = t \ln t t$ . At time t = 1, the position of the particle is x(1) = 6.
- (a) Write an expression for the acceleration of the particle.
  - (b) For what values of t is the particle moving to the right?
  - (c) What is the minimum velocity of the particle? Show the analysis that leads to your conclusion.
  - (d) Write an expression for the position x(t) of the particle.

1994 - AB5, BC2

- 5. A circle is inscribed in a square as shown in the figure above. The circumference of the circle is increasing at a constant rate of 6 inches per second. As the circle expands, the square expands to maintain the condition of tangency. (Note: A circle with radius r has circumference  $C = 2\pi r$  and area  $A = \pi r^2$ .)
  - (a) Find the rate at which the perimeter of the square is increasing. Indicate units of measure.
  - (b) At the instant when the area of the circle is  $25\pi$  square inches, find the rate of increase in the area enclosed between the circle and the square. Indicate units of measure.

2001: AB-4; BC-4

Let h be a function defined for all  $x \neq 0$  such that h(4) = -3 and the derivative of h is given by

 $h'(x) = \frac{x^2 - 2}{x} \text{ for all } x \neq 0.$ 

- (a) Find all values of x for which the graph of h has a horizontal tangent, and determine whether h has a local maximum, a local minimum, or neither at each of these values. Justify your answers.
- (b) On what intervals, if any, is the graph of h concave up? Justify your answer.
- (c) Write an equation for the line tangent to the graph of h at x = 4.
- (d) Does the line tangent to the graph of h at x = 4 lie above or below the graph of h for x > 4? Why?

2001: AB-2; BC-2





t	W(t)
(days)	(°C)
0	20
3	31
6	28
9	24
12	22
15	21

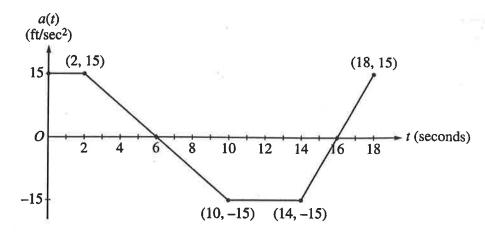
The temperature, in degrees Celsius ( $^{\circ}$ C), of the water in a pond is a differentiable function W of time t. The table above shows the water temperature as recorded every 3 days over a 15-day period.

- (a) Use data from the table to find an approximation for W'(12). Show the computations that lead to your answer. Indicate units of measure.
- (b) Approximate the average temperature, in degrees Celsius, of the water over the time interval  $0 \le t \le 15$  days by using a trapezoidal approximation with subintervals of length  $\Delta t = 3$  days.
- (c) A student proposes the function P, given by  $P(t) = 20 + 10te^{(-t/3)}$ , as a model for the temperature of the water in the pond at time t, where t is measured in days and P(t) is measured in degrees Celsius. Find P'(12). Using appropriate units, explain the meaning of your answer in terms of water temperature.
- (d) Use the function P defined in part (c) to find the average value, in degrees Celsius, of P(t) over the time interval  $0 \le t \le 15$  days.

2001: AB-3; BC-3







A car is traveling on a straight road with velocity 55 ft/sec at time t = 0. For  $0 \le t \le 18$  seconds, the car's acceleration a(t), in ft/sec<sup>2</sup>, is the piecewise linear function defined by the graph above.

- (a) Is the velocity of the car increasing at t = 2 seconds? Why or why not?
- (b) At what time in the interval  $0 \le t \le 18$ , other than t = 0, is the velocity of the car 55 ft/sec? Why?
- (c) On the time interval  $0 \le t \le 18$ , what is the car's absolute maximum velocity, in ft/sec, and at what time does it occur? Justify your answer.
- (d) At what times in the interval  $0 \le t \le 18$ , if any, is the car's velocity equal to zero? Justify your answer.